

## Scheduling and QoS scheduling

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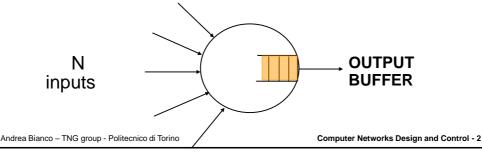
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# **Scheduling algorithms**

- Scheduling: choose a packet to transmit over a link among all packets stored in a given buffer (multiplexing point)
- Mainly look at QoS scheduling algorithms
  - Choose the packet according to QoS needs



## **Output buffered architecture**

- Advantage of OQ (Output Queued) architectures
  - All data immediately transferred to output buffers according to data destination
  - It is possible to run QoS scheduling algorithms independently for each output link
- In other architectures, like IQ or CIOQ switches, problems become more complex
  - Scheduling to satisfy QoS requirements and scheduling to maximize the transfer data from inputs to outputs have conflicting requirements

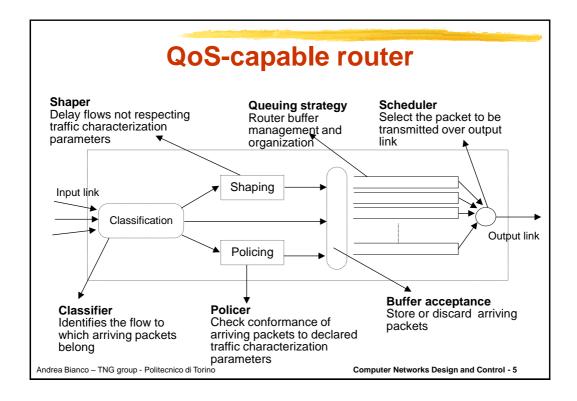
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# **QoS** scheduling algorithms

- · Operate over multiplexing points
- Micro or nano second scale
- Easy enough to be implemented in hardware at high speed
- Regulate interactions among flows
  - Single traffic relation (1VP/1VC)
  - Group of traffic relations (more VC/1VP o more VC with similar QoS needs)
  - QoS classes
- Strictly related and dependent from buffer management techniques
- To simplify and make the problem independent, assume infinite capacity buffers
- Choice of the scheduler may have implications on CAC

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## QoS scheduling algorithms: properties

- Flow isolation
  - "mis-behaving" (non conformant) flows should not damage "well-behaved" (conformant) flows
  - PER-FLOW queuing, which implies resource partitioning
    - · scheduler chooses from which queue to transmit the packet
  - Related to fairness
- · End-to-end statistical or deterministic guarantees
  - Bit rate
    - · Equal for all flows (useful for best effort traffic)
    - · Specific for each flow
  - Delay
  - Losses

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## QoS scheduling algorithms classification

- · Work-conserving scheduler
  - Always transmit a packet as long as there is at least a packet available in switch buffer
  - Optimal performance in terms of throughput
- Non-work-conserving scheduler
  - May delay packet transmission
    - · No transmission even if there are packets stored in buffers
  - Reduced throughput
  - Preserve traffic shape
    - · Better guarantees on delay jitter
      - Reduced buffer size
    - · May ease the CAC task
  - In theory appealing approach, not much used in practice

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# Scheduling discipline property

- Theorem
  - The sum of mean queuing delays received by a set of multiplexed connections, weighted by their share of the link load is independent of the (work conserving) scheduling algorithm
- A scheduling algorithm can reduce a connection mean delay only at the expense of increasing the delay of another connection
- A work-conserving scheduler can only reallocate delays among connections
- A non work-conserving scheduler can only provide a mean queuing delay larger than a work conserving discipline

# Work conserving versus non-work conserving schedulers

- Work-conserving schedulers disadvantage
  - Multiplexing point increase flow burstiness
    - · increase packet jitter and buffering requirments to prevent losses
  - Patological scenarios demonstrate that this phenomena may become worse when the number of crossed nodes increases
- Non work-conserving schedulers have buffering requirements largely independent of the network depth
  - Preserve traffic shape
  - May ease the CAC task

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## Scheduling algorithms goals

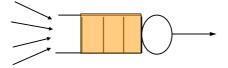
- Best-effort traffic scheduler
  - All active flows should obtain the same amount of service
  - Possibly max-min fair
  - No delay guarantees
  - FIFO, PS (Processor Sharing), RR (Round Robin), DRR (Deficit Round Robin)
- QoS scheduler, i.e. scheduler for traffic with QoS requirements
  - Specific bit rate guarantees for each flow
  - Specific delay guarantees for each flow
- Strict priority, GPS (Generalized Processor Sharing), WRR (Weighted Round Robin), WFQ (Weighted Fair Queuing), EDD (Earliest Due Date)

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#### **FIFO**

- FIFO (First In First Out) service discipline
  - Also known as FCFS (First Came First Served)
- Single queue
- Data queued according to arrival time and served in order



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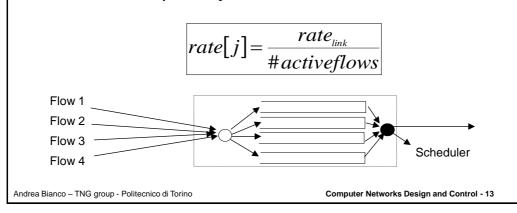
# **FIFO: properties**

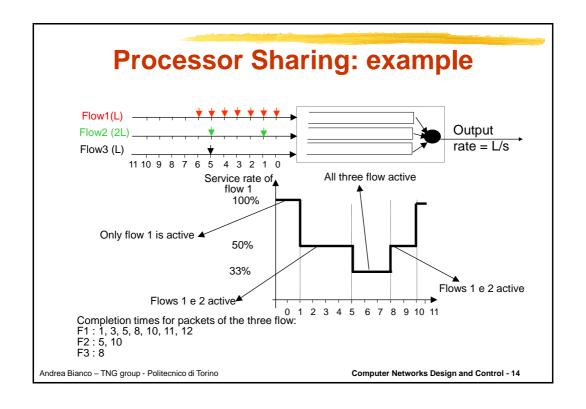
- Work-conserving
- Complete sharing of link bit rate and buffer space: no protection against non conformant flows
- All flows observe similar delay performance
  - Suited to best-effort traffic
- Neither bit rate (bandwidth) guarantees nor loss guarantees
  - Performance depend on the amount of ingress data traffic of each flow
- Aggressive flows obtain better performance
  - Unfair

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## **Processor Sharing**

- · Ideal work-conserving scheduler for best effort
- Each queue served according to a fluid model
- At time t, queue j is served at rate





## **Processor Sharing**

- Pros
  - If no data are discarded, a network of PS schedulers provides rates close to a max-min fair allocation
    - Rate of the max-min allocation only downstream from the bottleneck link
    - · Fairness does not require congestion control mechanisms
    - · If dropping packets, fair dropping must be ensured
- Cons
  - Ideal solution, non practical (packets are not fluids)
    - · Devise approximations

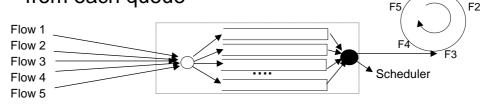
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#### **Round Robin**

- Processor sharing approximation
- Buffer organized in separate queues, one queue for each active flow
  - Each queue is a FIFO queue

 Service cycle among queues, one packet from each queue



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### **Round Robin**

- May have some delay bias
- To improve delay fairness, at each serving cycle it is possible to modify queue service order
  - At time 0, queue service order: 1,2,3,..,K
  - At time 1, queue service order: 2,3,..,K,1

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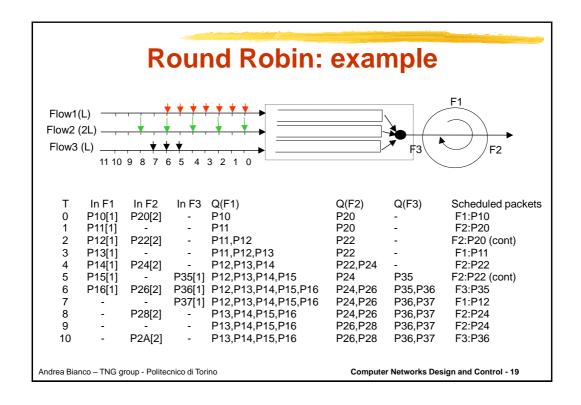
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# **Round Robin: properties**

- Relatively easy to implement in hardware
- Guarantees flow isolation
  - Through queue separation
- · Service rate of each queue:
  - C/K, for fixed packet size and k flows
  - For variable packet size, some rate unfairness may arise (fair in #packets per flow)
  - Taking into account packet size makes implementation more complex

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#### Scheduling in OQ architectures



#### **Deficit Round Robin**

- Round robin work conserving scheduler working with variable packet size
- One queue[i] per flow i
- The scheduler visits each queue in a round robin fashion
  - Each queue[i] has a deficit counter D[i] associated with
  - F[i] is increased by a fixed quantum when queue[i] is visited
  - Send the packet if D[i] large enough wrt packet size

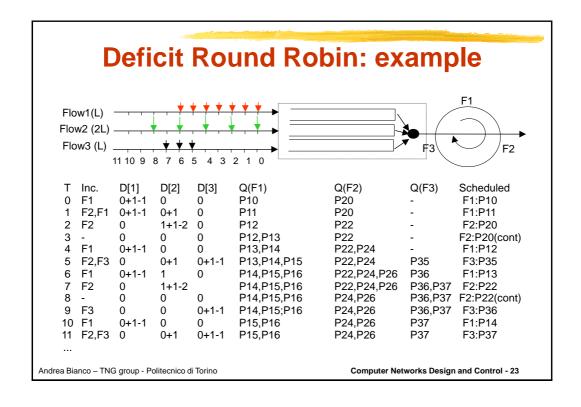
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## DRR: pseudo code

### **Deficit Round Robin**

```
if (length_first_packet of queue[i] > d[i])
{ packet is kept in queue[i] }
else
{packet transmitted on output link;
d[i]=d[i]- packet_length;
if (queue [i] is empty) { d[i]=0; }
```

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#### **Deficit Round Robin**

- The idea is to keep track of queues that were not served in a round (compute deficit) and to compensate in the next round
- Keep an active list of indices of queues that contain at least a packet to avoid examining empty queues
- May be a problem to define the quantum
  - If too small, may need to visit too many times queues before serving a queue
  - If too large, some short term unfairness may arise
- Fair only over a time scale longer than a round time
  - Round time is a function of the number of flows and packet size
  - At a shorter time scale, some flows may get more service
  - Small packet size or high transmission speed reduce the round time

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## **Strict priority**

- First attempt to define a QoS capable scheduler
- Buffer partitioned in k queues, k being the number of priority classes
- Each queue is associated with a different priority
- Data unit are stored in a queue according to their priority level
- Higher priority queue is always served. Only if empty, the lower priority is considered
  - Non preemptive service: packet under service finish transmission
- Within each queue, data are served according to a FIFO service discipline

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# Strict priority algorithm

- · Work-conserving
- Easy to implement
- Perfect isolation for high priority queue only, low priority queues may even suffer starvation (if CAC is not adopted on high priority queues)
  - Fair?
- · No bit rate, loss and delay guarantees
- No isolation among flows stored in the same FIFO queue, i.e., within the same priority level

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# **Generalized Processor Sharing**

- · Fluid system used as an ideal reference
- · One queue for each flow
- Each queue is served as if it contains a fluid flow, i.e. by an infinitesimal fraction of time
- Each queue j is associated with a weight w[j], normally derived from bit rate requirements
- At time t, queue j is served at rate:

$$rate[j] = rate_{link} \frac{w[j]}{\sum_{i=active avants} w[i]}$$

- A queue is active if it contains some fluid
- If the number of active flows decreases, excess bit rate is redistributed in proportion to queue weight
- CAC algorithms must control the rate of served flows, otherwise bit rate guarantees cannot be obtained

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## **GPS** properties

- Work conserving with flow isolation
- Per flow bit rate guarantees
  - When using a single GPS scheduler
  - When using a network of GPS schedulers
- End-to-end delay guarantees for token bucket (r,b) constrained flows
- · Provides bounds on buffer size
- Simple jitter delay guarantees ([0,Dmax])
- Ideal scheduler, practical approximations

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## **GPS** approximation

- Frame-based
  - Define a service cycle (frame)
  - Allocate frame portion to each flow
  - Example: WRR (Weighted-Round Robin),
     WDRR (Weighted Deficit Round Robin)
- Sorted priority
  - Compute a timestamp (tag) and associate it with each packet
  - Packets are ordered for increasing timestamp
  - Examples: Virtual Clock, WFQ (Weighted Fair Queuing), SCFQ

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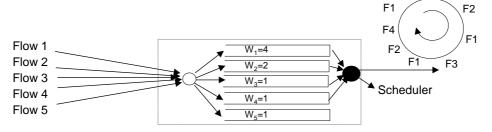
# **WRR: Weighted Round Robin**

- GPS approximation
- Buffer partitioned in N queues
  - each queue served according to a FIFO discipline
- A weight w<sub>i</sub> ∞ requested bit rate is associated with each queue
- A service cycle among queues is executed, each queue being served proportionally to its weight, i.e., w<sub>i</sub> per cycle
- Cycle length is the summation of the weights (possibly normalized)

$$\begin{array}{ccc}
1 & \longrightarrow & \parallel & W_1 \\
2 & \longrightarrow & \parallel & W_2 \\
N & \longrightarrow & \parallel & W_N
\end{array}$$

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# WRR: Weighted Round Robin



- · If all flows are active
  - F1 obtains 4/9 of the link bit rate
  - F2 obtains 2/9
  - F3, F4 and F5 obtain 1/9

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# **WRR:** properties

- Work-conserving
- · Flow isolation guaranteed
- For each queue i:
  - bit-rate =  $w_i / (\Sigma_i w_i) link_rate$ 
    - if all packets are of the same size
- Easy to implement (for a small number of flows)
- · Define a service cycle

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## **WRR: problems**

- · Service cycle (and fairness) may become long when
  - Many flows are active
  - Flows have very different weights
  - On a 45Mbit/s link, 500 flows with weight 1 and 500 flows with weight 10
    - Service time of one cell (48 ytes) 9.422us
    - A cycle requires 500+500\*10=5500 service time=51.82ms
- Service provided to flows may be bursty
  - Avoidable, but complex
- For each variation of the number of active flows (departure, arrival) service cycle must be redefined
  - How to deal with the remaining part of the cycle?
- To deal with variable packet size may use WDRR, Deficit Round-Robin extended to weight support
- · Note. WRR may be exploited in best effort scenario
  - May use weights in WRR to compensate for variable packet size for best effort traffic (requires knowledge of flow average packet size)

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## Sorted priority approximation to GPS

- Per-flow queuing
- Data (cells) served on the basis of negotiated rate and cell arrival time
  - Each data has a tag (urgency) assigned
- Data are inserted in a Sorted Priority Queue on the basis of data tag
- Data are served according to tag ordering
- Several algorithms: virtual clock, WFQ or PGPS, SCFQ

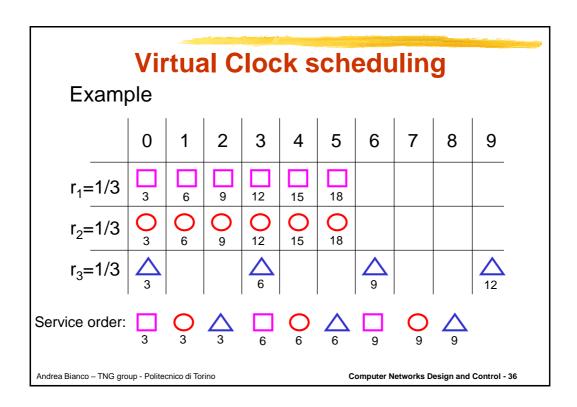
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## **Virtual Clock**

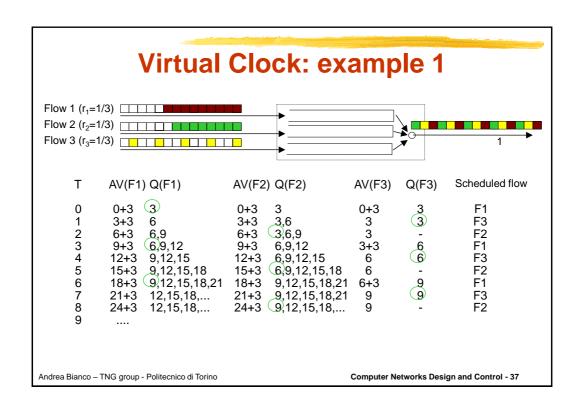
- · Time Division Multiplexing emulation
- Each flow j has an assigned normalized service rate r<sub>i</sub>, ranging from 0 to 1
- To each data k of flow j, whose length is L<sub>j</sub><sup>k</sup>, a tag (label, urgency, auxiliary virtual clock) is assigned
  - Tag represents the data finishing service time (starting service time + service time) in a TDM system serving flow j at rate r<sub>i</sub> link\_rate:

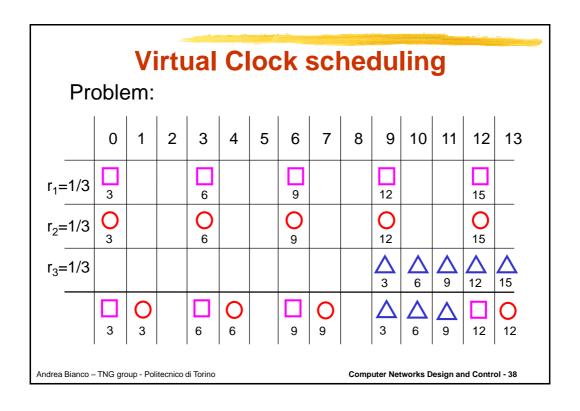
Aux 
$$VC_j^k = Aux VC_j^{k-1} + \frac{L_j^k}{r_j link_rate}$$

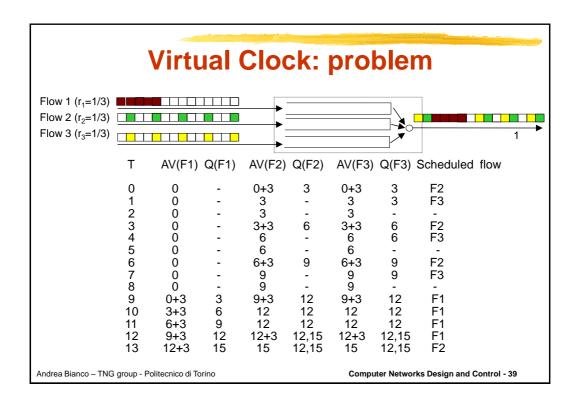
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#### Scheduling in OQ architectures







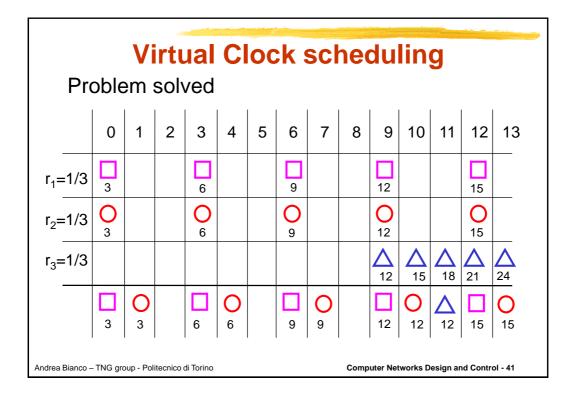
### **Virtual Clock**

- Long term fairness with some problems
  - Inactive flows "gain time" and get more service in the future, penalizing, and even starving, other active flows (even conformant flows)
  - Clock of different flows proceed independently
- Modify the tag computation, taking into account system real time:

Aux 
$$VC_j^k = max(Aux VC_j^{k-1}, a_j^k) + \frac{L_j^k}{r_i link_rate}$$

- where aik is the arrival time of cell k of flow j

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Modified Virtual Clock Another problem														
Time	0	1	2	3	4	5	6	7	8	9	10	11	12	13
r <sub>1</sub> =1/3	3	6	9	12	15	18	21	24	27	30	33	36	39	
r <sub>2</sub> =1/3	3	<b>O</b> 6	9	12	<b>O</b> 15	<b>O</b> 18	O 21	O 24	O 27	30	ж О	O 36	39	
r <sub>3</sub> =1/3													15	18
	3	3	6	<b>O</b> 6	9	9	12	O 12	15	<b>O</b> 15	18	<b>O</b> 18	15	18
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#### **Virtual Clock**

- Even the modified version of Virtual clock can lead to unfairness
- Clocks of flows are now synchronized by the system time
- However, tags may overcome the system time when flows get excess bandwidth
- Excess bandwidth must be redistributed among flows to ensure work conserving property but reallocation must not penalize flows in the future

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# WFQ (Weighted Fair Queueing) or PGPS (Packetized GPS)

- Algorithms that try to approximate GPS behavior
  - The minimum amount of service that can be provided cannot be smaller than the service time of a cell, since no preemption is admitted
- Many variations
  - Fair Queuing used in different context with different meaning
- At time  $\tau$ , the transmitted packet is the packet whose service would finish first in the GPS system if no other packets arrive after  $\tau$ 
  - Need to emulate the GPS system

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#### WFQ or PGPS

#### Example:

- 1 flow with negotiated rate 0.5
  - 10 fixed size packets arrive at rate 1 starting at time 1
- 10 flows with negotiated rate 0.05
  - 1 packet arrives at time 1

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 **Time** P5 P6 P7 P8 Ideal fluid P11 system GPS P20 P6 P7 P8 P9 P10 P11 P12 P13 P14 P15 P16 P17 P18 P19 P20 WFQ service order
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#### WFQ o PGPS

- Tag computation
  - Tag should represent the finishing service time of data in the GPS system
  - This time depends on the whole GPS system history until that data has ended its service
  - However, for practical reasons, it is fundamental to compute the tag when data units are received at buffer input
  - To compute the finishing time in the GPS at packet arrival, the future arrivals should be known, since the data finishing service time depends on flow activation in the future
  - The problem is trivial if all flows are always active, since service rate are fixed

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## **WFQ or PGPS**

• Tag computation for packet k of flow j:

$$\mathcal{F}_{j}^{k} = \max \{ \mathcal{F}_{j}^{k-1}, V(a_{j}^{k}) \} + \frac{L_{j}^{k}}{r_{j}}$$

where  $r_i = \phi_i \text{ link\_rate } | 0 < \phi_i < 1$ 

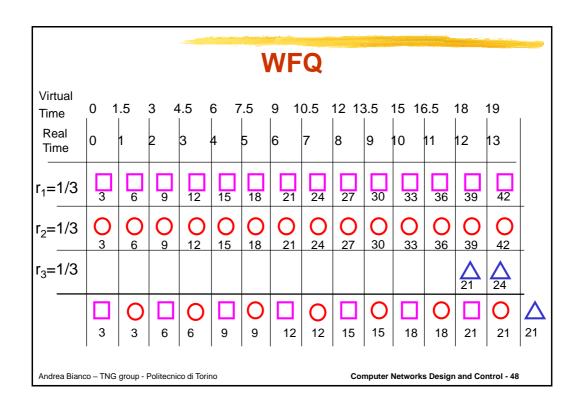
• V(t) is the system virtual time or system potential (w active flows): V(0) = 0

$$\frac{\partial V}{\partial \tau} = \frac{1}{\Sigma_{w} \phi_{w}}$$

computed at data arrival time aik

 If all flows are always active, the virtual time corresponds to the real time

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#### WFQ o PGPS

- · Very complex to implement
- Virtual time permits to compute tags at packet arrivals by "scaling" packet tags of arriving packets to ensure proper packet ordering, thus avoiding tag re-computation for packets already in the system
- Same properties of GPS
  - WFQ can emulate the ideal GPS system with a time difference bounded by the maximum size packet!
- Several variations were proposed
  - Indeed, in WFQ packets are never delayed too much, but could be transmitted too early
  - WF2Q
    - · improves the similarity of service order to GPS
    - among available packets, the packet with the smallest tag is chosen but only among packets whose service has already started in the ideal GPS system

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#### WFQ vs WF<sup>2</sup>Q 10 11 12 13 14 15 16 17 18 19 20 P3 P5 P2 P4 P6 P7 P8 P9 P10 **GPS** P11 P20 P9 P10 P11 P12 P13 P14 P15 P16 P17 P18 P19 P20 WFQ service order P18 P9 P19 P10 P20 P15 P6 P16 P7 WF<sup>2</sup>Q service order Andrea Bianco - TNG group - Politecnico di Torino Computer Networks Design and Control - 50

#### SCFQ

# (Self Clocked Fair Queueing)

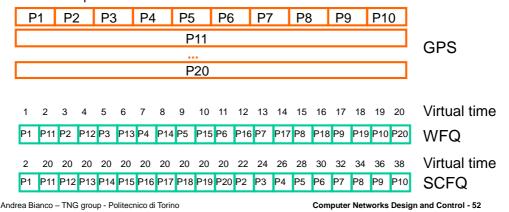
- Variation of PGPS, simpler to implement
- · Does not require emulation of GPS system
- · Uses a simplified virtual time
  - Virtual time is set to the tag of the packet being serviced

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#### SCFQ vs WFQ

- 1 flow with negotiated rate 0.5
  - 10 fixed size packets arrive at rate 0.5 starting at time 0
- 10 flows with negotiated rate 0.05
  - 1 packet arrives at time 0



## **Delay bounds**

- · Can be computed for token bucket limited flows (R,B)
- Guarantees independent of other flow behavior
- Max delay through n scheduler (excluding fixed delays):

$$\begin{array}{ll} - \ \mathsf{GPS} & \frac{B}{R} \\ - \ \mathsf{WFQ/PGPS} & \frac{B + n \cdot P_{\max}}{R} + \sum_{i=1}^n \frac{P_{\max}}{C_i} \\ - \ \mathsf{Virtual\ Clock} & \frac{B + n \cdot P_{\max}}{R} + \sum_{i=1}^n \frac{P_{\max}}{C_i} \\ - \ \mathsf{SCFQ} & \frac{B + n \cdot P_{\max}}{R} + \sum_{i=1}^n \frac{k_i \cdot P_{\max}}{C_i} \end{array} \quad \begin{array}{l} \bullet \ \mathsf{C_i\ output\ rate} \\ \bullet \ \mathsf{k_i\ number\ of\ flows} \\ \bullet \ \mathsf{P_{\max}\ maximum\ packet\ size} \end{array}$$

Bandwidth delay coupling

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## **EDD (Earliest Due Date)**

- In classical EDD
  - Each packet is assigned a deadline
  - Packets served in deadline order
  - Deadline satisfied only if the scheduler is not overcommitted
- Traffic divided in classes
  - Each class i is characterized by a service deadline d<sub>i</sub>
- Scheduler selects, at time t, the packet with the smallest residual time
  - Each packet is time stamped with time  $t_k$  on arrival
  - Residual time of a packet =  $t_k + d_i t$ 
    - the amount of time left before packet service deadline expires
- EDD tends to equalize the probability of violating the delay constraint

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## **EDD (Earliest Due Date)**

- Need to specify the process to assign deadlines
  - Delay EDD and Jitter EDD
- Delay EDD
  - packets belonging to sources obeying a peak rate constraint are assigned a worst case delay (in each node, deadline=expected arrival time+delay bound)
  - CAC must run a schedulability test to check if deadlines can be satisfied
  - Delay bound independent of bandwidth constraint (but need to reserve the peak)
- Jitter EDD
  - Delay jitter regulator in front of a EDD scheduler (non work conserving, see later)
- Issues
  - Interesting to manage delays, difficult to deal with bandwidth guarantees
  - Complex to implement (timers, dealing with real numbers)

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# Non work-conserving algorithms

- Packets can be scheduled only if eligible
- · Eligibility through traffic regulators
  - Rate-jitter regulator
    - · Bounds maximum rate
  - Delay jitter regulator
    - · Compensates for variable delay at previous hop
- After the regulator use a scheduler (may be FIFO)
- Properties
  - Reduced throughput
  - Worse average delays but
    - · Control on delay jitter
    - · Reduced buffer size
- Examples
  - Stop and go
  - Hierarchical round robin

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## Regulators for non work-conserving algorithms

- Rate jitter regulators
  - E.g.: peak rate regulator
    - eligibility time of a packet is the eligibility time of the previous packet plus the inverse of the peak rate (time taken to serve the packet at the peak rate)
- Delay jitter regulators
  - The sum of the queuing delay in the previous switch and the regulator delay is constant
    - · Eliminates the delay variability induced by the queuing delay at the previous hop
    - The output stream is a time shifted version of the traffic at input
    - · Time shift equal to propagation delay plus delay bound (worst case) at previous switch
  - Burstiness cannot build up
  - Do not protect against misbehaving sources
  - Very complex to implement (it requires clock synchronization)
- Note: by properly selecting the regulator and the scheduler a wide range of work-conserving and non work-conserving schedulers may be emulated
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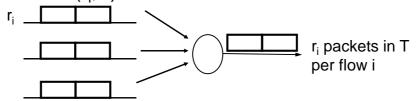
## An example of a non workconserving scheduler: Stop & go

- Framing strategy
  - Time axis divided into frames of length T
- At each switch, the arriving frame of each incoming link is mapped to the departing frame of the output link by a constant delay smaller than T
- Transmission of packets arriving on any link during a frame are postponed to the beginning of the next frame

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## Stop & go

- Packets on the same frame at the source stay in the same frame throughout the network
- If the traffic is (r<sub>i</sub>,T) smooth at source i, it will remain (r<sub>i</sub>,T) smooth



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# Stop & go

- As long as each node can ensure local delay bound, end-to-end delay bound can be guaranteed
- Problem of coupling between delay bounds and bandwidth allocations granularity
  - Assume a fixed packet size P
  - Minimum bandwidth can be P/T
  - Delay bounded by two time frames T
  - Reducing T, reduced the delay but increases the minimum bandwidth
- · Generalized stop&go with multiple frame sizes
  - Coupling still exist, but can have low delays for some flows and fine bandwidth granularity for other flows

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#### Scheduling in OQ architectures

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